

招生學年度	九十九	招生類別	轉學招生考試
系所班別	財務金融學系二年級		
科目	微積分		
注意事項	禁止使用掌上型計算機		

1. (20% , 各 10%) The following statements are “Yes” or “No”. If your answer is “No”, you should establish the counter example to support your answer.
- (1) If the function $f(x)$ has the limit at the point a , then the function $f(x)$ is continuous at the point a .
- (2) If the function $f(x)$ is continuous at the point a , then the function $f(x)$ has the derivative at the point a .

2. (15%) Using the concept of the signs ε and δ , prove that

$$\lim_{x \rightarrow 4} (3x - 5) = 7$$

3. (15%) Find the limit. Note: the function $[\]$ is the greatest integer function.

$$\lim_{x \rightarrow 3^+} [x^2 + 2x]$$

4. (12%) Find the derivative of the absolute function $|x|$, for $x \neq 0$.

5. (10%) Use the Chain Rule and the Implicit Differentiation to find $\frac{dy}{dx}$ if

$$y^3 + 6y = x^3$$

6. (12%) Determine a and b so that

$$f(x) = a\sqrt{x} + \frac{b}{\sqrt{x}}$$

has the point $(4, 13)$ as an inflection point.

7. (16% , 各 8%) Find the value

(1) $\frac{d}{dx} \int_{-x}^{x^2} \frac{e^t}{1+t} dt$

(2) $\int_0^1 xe^{2x} dx$